Thallium Nuclear Magnetic Relaxation in Solid Thallium(I) Thiocyanate TISCN: Phase Transition and Ionic Motion

Yoshihiro Furukawa and Daiyu Nakamura Department of Chemistry, Faculty of Science, Nagoya University, Nagoya, Japan

Z. Naturforsch. 45a, 1211-1216 (1990); received July 20, 1990

The NMR spin-lattice relaxation time (T_1) and linewidth parameter (T_2^*) of $^{203}\mathrm{Tl}$ and $^{205}\mathrm{Tl}$ in solid TISCN were measured from 290 K up to the melting point $(T_\mathrm{m}=507~\mathrm{K})$. The nonexponential magnetization recovery of T_1 could be characterized by a short (T_1^*) and a long (T_1^*) component. T_1^{1} showed a T^{-2} dependence below ca. 350 K in the orthorhombic phase $(T < T_\mathrm{c} = 371~\mathrm{K})$ and a minimum in the tetragonal phase $(T_\mathrm{c} < T < T_\mathrm{m})$, which were interpreted in terms of lattice vibrations and head-to-tail flips of the linear SCN ions, respectively. A broad minimum of T_1^* around 360 K was explained in terms of indirect nucleus-electron scalar coupling between $^{203}\mathrm{Tl}$ and $^{205}\mathrm{Tl}$, modulated via the anionic flips occurring in the symmetric and asymmetric potential fields for the high-and low-temperature phase, respectively. The phase transition is closely related to dynamical disorder of the anionic orientations. At higher temperatures, translational self-diffusion of Tl^+ was evidenced by the T_2^* and T_1^* results.

Introduction

It is known that many thiocyanate compounds with monovalent cations undergo interesting phase transitions [1–12]. Among them, the phase transition from orthorhombic to tetragonal KSCN is related to head-to-tail ordering of the rod-like SCN⁻ ions [1–8]. In the high-temperature phase, the anions jump between two equivalent orientations while in the low-temperature phase they form an ordered antiparallel arrangement [3, 7].

Thallium thiocyanate TISCN undergoes a phase transition at ca. 370 K [9, 10], where a mechanism similar to that of KSCN is assumed on the basis of the low- and high-temperature structures [10] and the entropy change of transition [9]. For solid TINO₂, the nuclear magnetic relaxation of Tl gives information on the motion of not only Tl⁺ but also the anions through the strong scalar coupling between 203 Tl and 205 Tl, modulated by the anionic motions [13]. In order to get similar information on TISCN, we measured its temperature dependences of the spin-lattice relaxation time (T_1) and linewidth parameter (T_2^*) of both 203 Tl and 205 Tl.

Reprint requests to Dr. Yoshihiro Furukawa, Department of Chemistry, Faculty of Science, Nagoya University, Nagoya 464-01, Japan.

Experimental

We used a pulse NMR spectrometer already reported [14]. T_1 was measured by the usual $180^{\circ}-t-90^{\circ}$ pulse sequence and T_2^* from the free induction decay signal. In order to identify the sample, DTA was carried out with a homemade apparatus [15] and X-ray powder analysis with a Shimadzu VD-1A diffractometer. Temperatures were determined within ± 1 K.

TISCN was prepared by mixing aqueous solutions of NH₄SCN and TIOH, subsequent heating to remove NH₃ gas [16] and recrystallization. For the NMR experiments, two types of the samples were used: One was finely powdered and the other partially melted to improve the filling factor. Because both samples yielded experimentally the same relaxation times, the NMR experiments were mainly carried out on the latter sample.

Experimental Results

From our DTA experiments we found the phase transition temperature $T_c = 371 \,\mathrm{K}$ and the melting point $T_m = 507 \,\mathrm{K}$. These values are in better agreement with $T_c = 372 \,\mathrm{K}$ and $T_m = 507 \,\mathrm{K}$ in [9] than those in [10]. The heat anomaly showed a long tail on the low-temperature side characteristic of a second-order phase transition, but a small latent heat was clearly observed indicating that the transition is of first order.

 $0932\text{-}0784 \,/\, 90 \,/\, 0900\text{-}1211 \,\$\, 01.30 / 0. - Please \ order \ a \ reprint \ rather \ than \ making \ your \ own \ copy$



Dieses Werk wurde im Jahr 2013 vom Verlag Zeitschrift für Naturforschung in Zusammenarbeit mit der Max-Planck-Gesellschaft zur Förderung der Wissenschaften e.V. digitalisiert und unter folgender Lizenz veröffentlicht: Creative Commons Namensnennung-Keine Bearbeitung 3.0 Deutschland

This work has been digitalized and published in 2013 by Verlag Zeitschrift für Naturforschung in cooperation with the Max Planck Society for the Advancement of Science under a Creative Commons Attribution-NoDerivs 3.0 Germany License.

Zum 01.01.2015 ist eine Anpassung der Lizenzbedingungen (Entfall der Creative Commons Lizenzbedingung "Keine Bearbeitung") beabsichtigt, um eine Nachnutzung auch im Rahmen zukünftiger wissenschaftlicher Nutzungsformen zu ermöglichen.

On 01.01.2015 it is planned to change the License Conditions (the removal of the Creative Commons License condition "no derivative works"). This is to allow reuse in the area of future scientific usage.

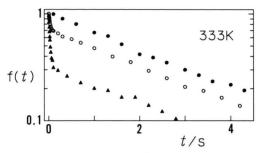


Fig. 1. Typical magnetization recovery curves $f(t) = \{M_0 - M_z(t)\}/c\,M_0$ in the T_1 measurements (16 MHz and 333 K). Here, M_0 represents the equilibrium value of the nuclear magnetization. c equals 1 or 2 for the saturation pulse method or the $180^{\circ}-t-90^{\circ}$ pulse method, respectively. \bullet and \circ : ^{203}Tl and ^{205}Tl for the $180^{\circ}-t-90^{\circ}$ pulse method, respectively. \bullet : ^{205}Tl for the saturation pulse method. Since the saturation pulses for ^{203}Tl or ^{205}Tl decouple magnetically the two spin systems because of their very close resonance frequencies [19], the magnetization recovery after the pulses becomes exponential.

The room-temperature NMR frequency of 205 Tl in solid TISCN was found to be low-field shifted by ca. 420 ppm as compared to that of an aqueous solution of TINO₃. The temperature dependence of T_1 of 203 Tl and 205 Tl was measured at the resonance frequencies 32 and 16 MHz. Except for above ca. 450 K and at 32 MHz, the magnetization recovery after the 180° pulse was very nonexponential. This may be due to the strong coupling of the spin systems of 203 Tl and 205 Tl, because of their resonance frequencies being very close [13, 17–20]. Typical magnetization recovery curves are shown in Figure 1. The nonexponential T_1 decay was decomposed into a long (T_1^1) and a short $(T_2^{\rm s})$ exponential relaxation time. The results are shown in Figure 2.

With increasing the temperature from room temperature, T_1^1 gradually decreased up to ca. 400 K, a change of the temperature coefficient being recognized near 350 K. In this temperature range, no frequency dependence was observed. On further heating, T_1^1 for 205 Tl at 16 MHz yielded a shallow minimum around 430 K, at 32 MHz a minimum of ca. 0.4 s near 460 K. It is noted that the T_1^1 minimum at the higher frequency is deeper than that at the lower frequency, in contrast to the expectation from the usual BPP theory of the magnetic dipolar relaxation [20]. When T_1^1 was measured at 32 MHz and above ca. 450 K, the magnetization recovery became almost exponential and gave a single T_1^1 value. In the whole temperature range studied, T_1^1 is likely to have no isotope dependence.

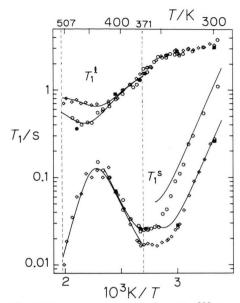


Fig. 2. Temperature dependence of the ²⁰³Tl and ²⁰⁵Tl spinlattice relaxation times in solid TISCN. Solid lines: Calculated with the theoretical expressions given in the text.

Symbols:		²⁰³ Tl	²⁰⁵ Tl
	16 MHz	-	♦
	32 MHz	•	0

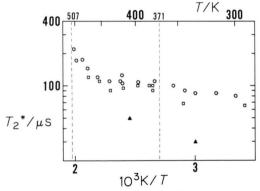


Fig. 3. Temperature variation of the linewidth parameter T_2^* .

Symbols:		²⁰³ Tl	205Tl
	16 MHz		0
	32 MHz		

On the other hand, T_1^s at 32 MHz sharply decreased with increasing temperature to ca. 350 K and became almost temperature independent from 350 K to T_c . A clear frequency dependence of T_1^s was observed in the room-temperature phase (phase II). For the high-tem-

perature phase (phase I), T_1^s at both 32 and 16 MHz increased with increasing temperature up to ca. 435 K. On further heating, T_1^s at 16 MHz sharply decreased while at 32 MHz it could not be determined, as mentioned above. In a narrow temperature range just above T_c , a small frequency dependence was recognized. T_1^s showed no isotope dependence in the whole temperature range studied as well.

Figure 3 shows the temperature variation of T_2^* . 205 Tl T_2^* at 16 MHz was almost constant at ca. 85 µs below 350 K and at ca. 110 µs between T_c and 450 K, and increased rather steeply above 450 K. T_2^* of 205 Tl at 32 MHz was slightly smaller than that at 16 MHz. For 203 Tl, T_2^* was found to be shorter by a factor of 2–3 than that of 205 Tl at a given frequency and temperature.

Analysis of the Results and Discussion

We will consider electron-nuclear magnetic coupling which is known to play an important role in Tl (I=1/2) NMR [13, 17–20]. Normal nuclear magnetic dipolar interaction can be neglected according to the usual BPP theory of T_1 for a model of complete motional averaging of the dipolar interactions [13, 20].

The nucleus-electron coupling of interest in solid TISCN is devided into two parts: The chemical shift interaction and the nucleus-electron indirect interaction. For the former interaction we are concerned only with its anisotropic part, and the relaxation rate $R^{\text{CSA}} \{=(T_1^{\text{CSA}})^{-1}\}$ due to this interaction is given by [20, 21]

$$R^{\text{CSA}} = (2/15) \,\omega^2 \,(\delta_{\parallel} - \delta_{\perp})^2 \,j(\omega), \tag{1}$$

$$j(\omega) = \tau/(1 + \omega^2 \tau^2). \tag{2}$$

Here, the chemical shift tensor is assumed to be axially symmetric and δ_{\parallel} and δ_{\perp} refer to the shielding along and perpendicular to the symmetry axis, respectively. ω stands for the Larmor frequency of ²⁰³Tl or ²⁰⁵Tl nuclei and τ is the correlation time of the time-dependent fluctuation of interest.

The nucleus-electron indirect interaction can be subdivided into scalar (or exchange) and pseudodipolar terms. The scalar coupling between unlike spins contributes to the second moments as well as to the relaxation but the one between like spins does not [17-20, 22]. The relaxation rate of spin $i(R_i^{SC})$ due to

the scalar interaction is [20]

$$R_i^{\text{SC}} = (2/3) \sum_i A_{ij}^2 S_j (S_j + 1) j (\omega_i - \omega_j),$$
 (3)

where A_{ij} is the scalar coupling constant, in units of rad/s, between i and unlike j spins, of which the Larmor frequencies are expressed by ω_i and ω_j , respectively, and S_j is the spin quantum number of spin j. The sum of A_{ij}^2 can be expressed by the second moment of i spins due to the same interaction by [17-19]

$$\langle \delta \omega^2 \rangle_i^{\text{SC}} = (1/3) \sum_j A_{ij}^2 S_j (S_j + 1).$$
 (4)

From the natural abundances of the Tl isotopes, $\langle \delta \omega^2 \rangle_{203}^{SC}$ is expected to be 2.4 times larger than $\langle \delta \omega^2 \rangle_{205}^{SC}$. The observed ratio of T_2^* shows that the dominant interaction in solid TISCN is the scalar one.

The pseudodipolar term can be approximated by the same expression as that for the normal dipolar interaction except for its coupling constant, and these two interactions are combined into a single term [18, 19]. For several Tl-containing compounds, the scalar interaction is estimated to be larger than the pseudodipolar interaction as well as than the normal dipolar interaction between Tl nuclei [17–19]. In the following discussion we neglect the pseudodipolar interaction as well.

Because the two spin systems of ²⁰³Tl and ²⁰⁵Tl couple to each other, the observed relaxation rates are the eigen values of the following relaxation matrix [17, 20]:

$$\begin{pmatrix} -R^{\text{CSA}} - R^{\text{SC}}_{203} & R^{\text{SC}}_{203} \\ R^{\text{SC}}_{205} & -R^{\text{CSA}} - R^{\text{SC}}_{205} \end{pmatrix}.$$
 (5)

Here, R^{CSA} is assumed to be the same for ^{203}Tl and ^{205}Tl , and a small difference (less than 1%) in their gyromagnetic ratios is neglected for simplicity. As a result, one can obtain two characteristic T_1 values:

$$(T_1^s)^{-1} = R^{CSA} + R^{SC}, (6)$$

$$(T_1^1)^{-1} = R^{CSA}, (7)$$

where

$$R^{\rm SC}\!=\!R^{\rm SC}_{203}\!+\!R^{\rm SC}_{205}\!=\!2\,(C^{\rm SC})^2\,j\,(\omega_{203}\!-\!\omega_{205}),\;(8)$$

$$C^{\text{SC}} = (\langle \delta \omega^2 \rangle_{203}^{\text{SC}} + \langle \delta \omega^2 \rangle_{205}^{\text{SC}})^{1/2}. \tag{9}$$

Therefore, the observed relaxation times, T_1^s and T_1^l , become isotope independent. This is the case, as described in the previous section.

As discussed later, T_1^1 below 350 K is likely to change as

$$(T_1^1)^{-1} = KT^2. (10)$$

This type of T_1 behavior may be assigned to the relaxation by lattice vibrations via a Raman-like process [13, 17, 20]. Therefore, the contribution of (10) is added to (7).

Now, we will consider the correlation time τ of the head-to-tail flip of the linear SCN $^-$ ions in the TISCN crystal, which is the most interesting motion in the phase transition. Phase I of TISCN is tetragonal with the space group I4/mcm [10]. The site symmetries require that the SCN $^-$ ion in phase I is disordered between two equivalent orientations, implying that the anionic head-to-tail flip is occurring between symmetric potential wells. Even in phase II, the flip is assumed to go on, but it occurs between unequal potential wells.

Simplified potential curves are shown in Figure 4. Between the asymmetric potential wells for phase II, the SCN $^-$ ion jumps with a rate W from a favored to unfavored orientation and with a rate aW in the opposite direction.

$$W = k \exp\left\{-(E_a + \Delta E)/RT\right\},\tag{11}$$

$$a = \exp\left(2\,\Delta E/RT\right). \tag{12}$$

The usual Arrhenius relation is used for the jump rates. The parameter a represents the ratio of the statistical probabilities that the SCN⁻ ion occupies the favored and the unfavored orientation and is related to the order parameter η by

$$\eta = (a-1)/(a+1). \tag{13}$$

The correlation time of the motion is defined as

$$\tau^{-1} = W + a W, \tag{14}$$

$$\tau = \tau_0 \exp \{ (E_a + \Delta E) / RT \} / (1+a). \tag{15}$$

Finally, the observed T_1^{-1} given by (6) and (7) should be corrected by a factor of $4 a/(1+a)^2$ because of the smaller occupancy of the unfavored orientation [23]. For the symmetric potential, of course, $\Delta E = 0$, a = 1, and $\eta = 0$.

T_1^1 in Phases I and II

The temperature dependence of T_1^1 can be separated into two regions: The low-temperature region where T_1^1 shows no frequency dependence and the high-tem-

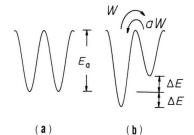


Fig. 4. Scheme of the potential curves for the head-to-tail flip of an SCN⁻ ion (a) in the disordered high-temperature phase I and (b) in the ordered low-temperature phase II.

perature region where T_1^1 has a frequency dependent minimum. At temperatures below 350 K, T_1^1 changed according to (10), where $K = 3.4 \cdot 10^{-6} \, \mathrm{s}^{-1} \, \mathrm{K}^{-2}$, and is attributed to the lattice vibrations. The relaxational behavior given by (10) is frequently observed in T_1 for nuclei with $I \ge 1$ having a nuclear electric quadrupole moment [24]. Because both Tl nuclei have no quadrupole moment, the interactions modulated by the lattice vibrations are of magnetic origin, maybe due to indirect nucleus-electron interactions between the Tl nuclei, which depend on Tl-Tl distances more strongly than the normal dipolar ones [18].

The T_1^1 minima in phase I are characteristic for relaxation due to the chemical shift anisotropy given by (1). The temperature and frequency dependence of T_1^1 were analyzed in this line, and the motional parameters responsible for the T_1^1 minima were determined by a least-squares fitting of (1) and (10). The numerical results are listed in Table 1, and the calculated T_1^1 dependence is given in Figure 2. It is reasonable to assign the observed E_a and τ_0 to the head-to-tail flips of the SCN $^-$ ions because translational self-diffusion of the Tl $^+$ ions was detected through T_1^s as discussed later.

It is still not clear whether the cation in phase I exists in ordered positions or not [3, 7, 10]. Two models are proposed: One implies that Tl^+ is fixed at 0, 0, 1/4 sites on the crystal C_4 axis, and the other assumes that the cation occupies four sites statistically and dynamically with equal occupancy 1/4. The four sites are slightly displaced from the 0, 0, 1/4 site and related to each other by the C_4 symmetry. Here, we observed a rather large effect from the chemical shift anisotropy on Tl T_1 . This fact excludes the former model for the Tl^+ positions, because the chemical shift tensor for the Tl^+ ion fixed on the C_4 axis is invariant under the simple 180° flip of the anions. Therefore, the

Phase	T_1	$\frac{ \delta_{\parallel} - \delta_{\perp} }{\text{ppm}}$	$\frac{C^{\text{sc}}}{\text{krad/s}}$	$\frac{E_a}{\text{kJ mol}^{-1}}$	$\frac{2\Delta E}{\text{kJ mol}^{-1}}$	$\frac{\tau_0}{10^{-14} \text{ s}}$	$\frac{K}{10^{-6} \mathrm{s}^{-1} \mathrm{K}^{-2}}$
I	T_1^1	341	_	50.5	0	1.70	4.0
	$T_1^{\mathbf{s}}$	_	9.0	54.4	0	1.98	_
II	T_1^1	_	_	_	_	_	3.4
	T_1^{s}	_	9.0 a	54.4 a	5.5 b	1.98 a	_

Table 1. Motional parameters in solid TISCN.

^b This is fixed below 325 K.

TI⁺ ion in phase I should be disordered dynamically over the four positions. This conclusion supports the model of positional disorder of TI⁺ or the "dynamical twinning model" [10]. Then the direct origin of the modulation of the chemical shift anisotropy at the TI sites may be attributed to a local hopping of the TI⁺ ions, which is closely correlated to the head-to-tail flips of the SCN⁻ ions.

$T_1^{\rm s}$ in Phase I

The temperature dependence of T_1^s between T_c and 435 K in phase I can be analyzed in terms of the same model as above, but the interaction considered is scalar. The theoretical T_1^s is given by (6), indicating no isotope but frequency dependence. By fitting (6) to the data in this temperature region, three motional parameters C^{SC} , τ_0 , and E_a were determined. τ_0 and E_a determined from T_1^s are in reasonable agreement with those from T_1^1 . Thus, we could determine the motional parameters of the anionic flips indirectly through the TI NMR relaxations. An E_a value of the SCN⁻ ion flip has been determined for KSCN by means of the temperature dependence of the Raman linewidth [5] and 39 K T_1 [8] as ca. 40 kJ mol⁻¹. The value of 51– 54 kJ mol⁻¹ for TISCN is somewhat large in comparison with that for KSCN. This may reflect the smaller c axis of phase I of TISCN compared to KSCN [7, 10], taking into account that out-of-plane flips of the SCN⁻ ions are dominant rather than in-plane ones

Above 435 K in phase I, T_1^s at 16 MHz decreased sharply with increasing temperature. This T_1^s decrease is assignable to the translational self-diffusion of Tl⁺ ions, because a substantial motional narrowing was observed in the temperature dependence of T_2^* in the same temperature range (Figure 3). To confirm this, we preliminarily measured the electrical conductivity by an ac impedance method and found it to be as high as $2 \cdot 10^{-4}$ S m⁻¹ at ca. 460 K, supporting the occurrence of rapid ionic diffusion. The E_a value of the Tl⁺

ionic diffusion was roughly estimated from T_1^s to be 90 kJ mol⁻¹. This E_a value in TISCN is comparable with 77 kJ mol⁻¹ for the high-temperature phase of TINO₃ [17] but much smaller than 48 kJ mol⁻¹ in the high-temperature phase of TINO₂ [13]. The small value for the latter compound is attributable to the fact that its conducting phase is an ionic plastic phase [25].

T_1^s in Phase II and the Order Parameter

Since T_1^s changes smoothly through T_c and shows a flat minimum below T_c , it is obvious that the SCN⁻ ion is still rapidly flipping even in the low-temperature ordered phase I. The interaction responsible to the T_1^s relaxation is also the scalar one, but the potential curve for flips becomes asymmetric as shown in Figure 4b. The analysis of the T_1^s data can be made by using (6) and (13–15) to determine the unknown parameters E_a , τ_0 , $C^{\rm SC}$, and ΔE .

First, we tried to fit the theoretical T_1^s to the observed ones, adjusting the above four constants. The calculations gave a good fitness between the experimental and observed curves but yielded a unreasonably large CSC value (ca. 480 k rad/s), compared with 9.0 k rad/s for phase I and also with the values reported for TINO₂ [13], TICl [19], or TINO₃ [17]. Therefore, this model calculation was disregarded. Secondly, we adopted a model for which ΔE is temperature dependent. This model is closely related to the order-disorder transition mechanism. For the simplicity of the analysis and also to retain the continuity of the $T_1^{\rm s}$ through $T_{\rm c}$, we assumed that the values of $C^{\rm SC}$, E_a , and τ_0 are the same as the corresponding ones determined from T_1^s in phase I. Then, we calculated the theoretical T_1^s to fit the low-temperature portion of the observed T_1^s by varying ΔE . This procedure implies that ΔE is temperature independent at temperatures much below T_c . The T_1^s curves thus obtained are drawn in Figure 2. The temperature dependent ΔE or η can be estimated from the difference between the

^a These are taken to be equal to the corresponding ones determined from T_1^s in phase I.

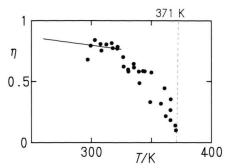


Fig. 5. Temperature dependence of the order parameter η determined from T_1^s for phase II of TISCN. The curve below 325 K is calculated from (12) and (13) with a temperature independent $2 \Delta E$ of 5.5 kJ mol^{-1} .

observed and calculated T_1^s , and the result is shown in Figure 5. The η vs. T curve indicates a first-order phase transition.

 M. Sakiyama, H. Suga, and S. Seki, Bull. Chem. Soc. Japan 36, 1025 (1963).

[2] Y. Kinsho, N. Onodera, M. Sakiyama, and S. Seki, Bull. Chem. Soc. Japan 52, 395 (1979).

[3] Y. Yamada and T. Watanabe, Bull. Chem. Soc. Japan 36, 1032 (1963).

[4] Z. Iqbal, L. H. Sarma, and K. D. Möller, J. Chem. Phys. 57, 4728 (1972).

[5] F. J. Owens, Solid State Commun. 29, 789 (1979).

[6] S. Yamamoto, M. Sakuno, and Y. Shinnaka, J. Phys. Soc. Japan 56, 2604 (1987).

[7] S. Yamamoto, M. Sakuno, and Y. Shinnaka. J. Phys. Soc. Japan 56, 4393 (1987).

[8] B. Topič, U. Haeberlen, R. Blinc, A. Fuith, and H. Warhanek, Solid State Commun. 72, 151 (1989).

[9] W. Klement, Jr., Bull. Chem. Soc. Japan **49**, 2148 (1976).

[10] R. Lippman and R. Rudman, J. Chem. Phys. **79**, 3457 (1983).

[11] S. Manolatos, M. Tillinger, and B. Post, J. Solid State Chem. 7, 31 (1973).

[12] T. Tanabe, R. Ikeda, and D. Nakamura, Phys. Stat. Sol. a 114, K 143 (1989).

[13] Y. Furukawa and H. Kiriyama, Chem. Phys. Lett. 93, 617 (1982).

In conclusion, the temperature dependence of the Tl spin-lattice relaxation times in solid TISCN can be analyzed in terms of the chemical shift anisotropy at the Tl nuclei and the scalar interaction between the ²⁰³Tl and ²⁰⁵Tl nuclei modulated by the head-to-tail flips of the linear SCN⁻ ions. The motional parameters of the anionic flip were determined indirectly from the Tl T_1^s and T_1^l for the high-temperature phase I. For the low-temperature phase II, the order parameter of the SCN⁻ ion orientation could be determined, confirming the order-disorder nature of the phase transition. It should be emphasized, however, that the order parameters are derived under several assumptions and have large scatter because of the difficulty in determining T_1^s precisely from the nonexponential T_1 recovery.

[14] S. Gima, Y. Furukawa, R. Ikeda, and D. Nakamura, J. Mol. Struct. 111, 189 (1983).

[15] Y. Kume, R. Ikeda, and D. Nakamura, J. Magn. Resonance 33, 331 (1979).

[16] M. M. Markowitz, J. Org. Chem. 22, 983 (1957).

[17] M. Villa and A. Avogadro, Phys. Stat. Sol. **b75**, 179 (1976).

[18] N. Bloembergen and T. J. Rowland, Phys. Rev. 97, 1679 (1955).

[19] S. Clough and W. I. Goldburg, J. Chem. Phys. 45, 4080 (1966).

[20] A. Abragam, The Principles of Nuclear Magnetism, Oxford Univ. Press, Oxford 1961, Chapter 8.

[21] T. C. Farrar and E. D. Becker, Pulse and Fourier Transform NMR, Academic Press, New York 1971, Chapter 4

22] J. H. Van Vleck, Phys. Rev. 74, 1168 (1948).

[23] D. C. Look and I. J. Lowe, J. Chem. Phys. **44**, 3437 (1966).

[24] H. Chihara and N. Nakamura, Adv. Nucl. Quadrupole Resonance 4, 1 (1980).

[25] K. Moriya, T. Matsuo, and H. Suga, J. Phys. Chem. Solids 44, 1103 (1983).